

# Efficient Answering of Set Containment Queries for Skewed Item Distributions

Manolis Terrovitis  
IMIS, RC Athena  
Greece  
mter@imis.athena-  
innovation.gr

Panagiotis Bouras  
NTU Athens  
Greece  
pbour@dblab.ece.ntua.gr

Panos Vassiliadis  
Univ. of Ioannina  
Greece  
pvassil@cs.uoi.gr

Timos Sellis  
NTU Athens and IMIS, RC  
Athena  
Greece  
timos@imis.athena-  
innovation.gr

Nikos Mamoulis  
Univ. of Hong Kong  
PR of China  
nikos@cs.hku.hk

## ABSTRACT

In this paper we address the problem of efficiently evaluating containment (i.e., subset, equality, and superset) queries over set-valued data. We propose a novel indexing scheme, the Ordered Inverted File (OIF) which, differently from the state-of-the-art, indexes set-valued attributes in an ordered fashion. We introduce query processing algorithms that practically treat containment queries as range queries over the ordered postings lists of OIF and exploit this ordering to quickly prune unnecessary page accesses. OIF is simple to implement and our experiments on both real and synthetic data show that it greatly outperforms the current state-of-the-art methods for all three classes of containment queries.

## Categories and Subject Descriptors

E.2 [Data Storage Representations]: Composite structures

## General Terms

Algorithms, Experimentation

## Keywords

Inverted files, containment queries, set-values, ordered inverted files

## 1. INTRODUCTION

Containment queries are meaningful whenever we need to examine membership properties (e.g. which records contain items  $a$  and  $b$ ?) in collections of data. When posing a containment query we treat the underlying data as collections of sets, but data can be modelled in various ways; they can be set-values, they can span in several tuples of a relational table, or they can be XML documents with additional structural information. The efficient evaluation of

containment queries is an important issue in several application areas, e.g., in market basket analysis the transactional logs of customers are examined to retrieve those that contain certain items. In this work we focus on three fundamental containment operators: subset, set-equality and superset and we propose an inverted file based index, which efficiently addresses skewed item distributions.

In the research literature there are two main classes of access methods specialized for supporting containment queries: signature files [13] and inverted file indices [24, 49]. Surveys have shown that inverted files outperform signature-based methods for containment queries on low cardinality set-values [20] and on text documents [48]. Moreover, inverted files have been shown to outperform traditional relational methods (B-trees) for containment queries in most cases [46]. Considering inverted files as the state-of-the-art mechanism for set containment is also supported by the fact that they are being used by all WWW search engines [45].

Nevertheless, the performance of inverted files suffers when the size of the indexed dataset becomes very big compared to the domain, or when the distribution of the items is skewed. In these cases, some inverted lists become very long and compromise the performance of query evaluation. This is due to the fact that the evaluation algorithms resolve to merge-joins between the lists. Huge collections of low cardinality set-values from a limited or skewed domain of items, appear often in practice. From the statistics provided by the US Food Marketing Institute [22], we infer that only in 2005, there have been almost 18 billion transactions (i.e., sets of products bought at a time), in US supermarkets, with the average supermarket having 45k different products. Indexing such data with inverted files to provide efficient containment query evaluation (as part of market analysis tasks) would be the best solution available, but still the performance would not be satisfactory. The problem is further augmented by the fact that users usually pose queries involving the most frequent items in the dataset [7].

To compensate for this shortcoming, we propose a novel indexing scheme, the Ordered Inverted File (OIF). OIF first orders the set-values according to their items and then indexes them similarly to the classic inverted file. The ordering of the set-values confines the merge-join only to continuous subsets of the inverted lists that are relevant to the queries. Since these subsets are in fact ranges over the ordered set-values, OIF employs B-trees to index them and further prune the number of disk pages that need to be retrieved from the hard disk.

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. To copy otherwise, to republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee.

EDBT 2011, March 22–24, 2011, Uppsala, Sweden.

Copyright 2011 ACM 978-1-4503-0528-0/11/0003 ...\$10.00

The primary goal of OIF is to reduce the I/O cost for containment queries. Our approach focuses on non-textual set-valued data, that become more and more apparent in practice, e.g., transactions from retail stores, web logs etc. This kind of data is characterized by skewed distributions and a large ratio between the number of transactions and the size of the items’ domain. We assume a context where the main memory is limited and the index cannot be memory resident. Many systems employing inverted files are systems dedicated to answering a single type of queries (e.g., superset in publish/subscribe systems) and they can afford using only memory resident indices. If there is sufficient memory, the basic cost in query answering is the CPU cost and specialized techniques like skip lists [34], or other memory resident structures [25] are used to reduce this cost. On the other hand, in this work we focus on containment queries under limited memory budgets. This is the case of a database that contains both the set-valued data and other information and has to respond to various types of queries. As our experiments demonstrate the I/O cost is dominant in evaluating containment queries, if the index is disk resident. We stress that the proposed approach is not a panacea for all kinds of settings and queries: therefore, we do not consider textual data sets that are traditional in IR and have very different characteristics; we do not consider specialized systems that can afford to have all the indices in main memory; we also do not consider approximate or ranking (i.e., similarity) queries.

In short, our contributions are:

- We propose a novel indexing scheme, the ordered inverted file (OIF), which outperforms the current state-of-the-art for containment queries. Our proposal is simple to implement and provides superior performance in all cases.
- We provide new evaluation algorithms for subset, set-equality and superset queries that take advantage of the proposed index.
- We show that the OIF performs reduced disk I/O operations compared to the classic inverted file and scales significantly better. Moreover, we test OIF’s performance with an implementation that is built on the Berkeley DB embedded database, and we assess our proposal by extensive experiments on both real and synthetic data.

The rest of the paper is organized as follows: Section 2 provides the problem setting and the necessary background. In Section 3, we present the structure of the OIF index. In Section 4, we present the query evaluation algorithms and discuss their performance. Section 5 includes our experimental evaluation, and Section 6 places our contribution with respect to related works. Finally we conclude the paper in Section 7.

## 2. BACKGROUND

Consider a database  $D$ , where each record  $t$  has two fields: a unique key  $t.id$  and a set-valued attribute,  $t.s$ . There are more than one ways to store such data. In the *object-relational* model, attributes are allowed to be set-valued, therefore we can store  $D$ , as a table with two attributes  $t.id$  and  $t.s$ , as described above and depicted in (Fig. 1). In the pure relational model, set-valued attributes correspond to a set of tuples, therefore  $D$  is modeled as a table with two attributes  $id$  (which is no longer a key) and  $item$ , which takes a single value. For example, in this model, the first tuple of Fig. 1 would be represented as four tuples  $(101, g)$ ,  $(101, b)$ ,  $(101, a)$ , and  $(101, d)$ . Our method applies to both data organizations; for simplicity, in the rest of this paper we will assume the

$id$	$s$	$id$	$s$	$id$	$s$
101	{g, b, a, d}	107	{d, h}	113	{a}
102	{a, e, b}	108	{b, a, f}	114	{a, d}
103	{f, e, a, b}	109	{b, c}	115	{j, c, a}
104	{d, b, a}	110	{j, b, g}	116	{i, c}
105	{a, b, f, c}	111	{a, c, b}	117	{a, c, h}
106	{c, a}	112	{i, d}	118	{d, c}

Figure 1: Exemplary relation  $D$

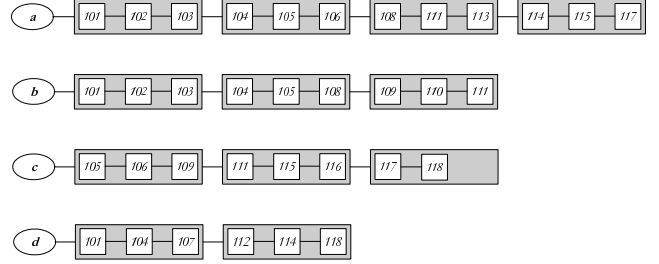


Figure 2: Partially shown IF for the example of Fig. 1.

object-relational one. The active domain of  $t.s$  is a finite set of values denoted as *vocabulary*  $I$  (i.e., the values  $a, b, c, d, e, f, g, h, i, j$  for the database of Fig. 1).

**Queries.** In set containment queries, the user specifies a query predicate and a *query set*  $qs$ . The queries we are interested in are the following:

- *Subset queries.* In subset queries the user asks for all records  $t$  that contain the query set  $qs$ , i.e.,  $\{t \mid t \in D \wedge qs \subseteq t.s\}$ .
- *Equality queries.* In equality queries the user asks for all records, whose set-value is identical to the query set, i.e.,  $\{t \mid t \in D \wedge qs \equiv t.s\}$ .
- *Superset queries.* In superset queries the user asks for all records, whose items are all contained in the query set, i.e.,  $\{t \mid t \in D \wedge qs \supseteq t.s\}$ .

As an example, assume that the data of Fig. 1 are the entries of a web log that trace the areas visited in a specific portal. Each record represents a different user session, and items in  $I$  (i.e.,  $a, b, c$ , etc.) model URLs. The containment queries have intuitive meanings in all cases, e.g., “Which users limited their visit in the portal in the main and downloads sections?” (superset query).

**Inverted files.** The inverted file [24, 49] is composed by two main parts: (a) the *vocabulary table*, which contains all distinct items that appear in the database, and (b) one *inverted list* for each item, which includes references to the sets that contain the item. The inverted lists of four items ( $a, b, c$ , and  $d$ ) from the database of Fig. 1 appear in Fig. 2. The gray boxes in Fig. 2 represent disk pages. The inverted lists can be very long for large databases, therefore it is natural to assume that they are stored in the secondary storage, while the vocabulary can fit in main memory. The latter is usually organized as an array, with a link from each entry to the inverted list, which contains references to all sets that include the respective item. Inverted lists are placed in contiguous regions in the disk, since querying requires to retrieve the whole lists that are linked to the query items [26].

A subset query  $qs$  is evaluated by fetching the inverted lists of all items in  $qs$  and intersecting them. This computes the records that contain *all* items in  $qs$ . For example, applying the subset

$id$	Items	$id$	Items	$id$	Items
1	{a}	7	{a, b, f, e}	13	{b, c}
2	{a, b, c}	8	{a, b, e}	14	{b, g, j}
3	{a, b, c, f}	9	{a, c}	15	{c, d}
4	{a, b, d}	10	{a, c, h}	16	{c, i}
5	{a, b, d, g}	11	{a, c, j}	17	{d, i}
6	{a, b, f}	12	{a, d}	18	{d, h}

Figure 3: Example relation  $D$  with sorted ids

query  $qs = \{a, d\}$  returns  $\{101, 104, 114\}$ , which are indeed the only records in  $D$  containing both  $a$  and  $d$ . For processing equality and superset queries, the inverted file is extended, so that for each record-id in an inverted list, we also store the length (i.e., cardinality)  $l$  of the respective set [20]. An equality query  $qs$  is then processed in exactly the same way as a subset query, but records with cardinality different than  $qs.l$  are directly pruned while traversing the lists. A superset query is processed by computing the union of the inverted lists for the  $qs$ -items (as opposed to their intersection for subset queries). While merging, we count the number of occurrences of each id in these lists. If for a record this number is equal to its length then we know that the record is a result to the superset query (since the record does not contain any items outside  $qs$ ). For example, the superset query  $qs = \{a, c\}$  returns records 106 and 113, since (i) these records appear in the inverted lists of either  $a$  or  $c$  and (ii) their cardinalities equal their occurrences in the inverted lists (e.g., 106 has two values and appears in both inverted lists).

### 3. THE ORDERED INVERTED FILE

Our proposal, the *ordered inverted file* (OIF) is an extension of the classic inverted file, based on the introduction of an ordering for the database items and records. Examples of possible item orderings include the ordering by frequency, alphanumeric value, etc. Later in the paper, we demonstrate that when containment queries are posed, this ordering allows the identification of specific areas in the inverted lists that contain potential answers to the queries. By coupling this property with a B-tree that organizes the lists as blocks in sequential disk pages, we are able to significantly decrease disk page accesses in query evaluation.

In terms of structure, the *ordered inverted file* (OIF) index comprises the following:

1. An inverted file, where the inverted lists contain references to the database records, according to a special ordering.
2. A B-tree, which organizes the access to all the parts of each inverted list. The search key of the B-tree is based on the value of the last record referenced in the corresponding block.

**Ordering of the inverted lists.** The ordering we adopt in this work for the records is based on the ordering of the items of the vocabulary  $I$ . Let the support  $s()$  be a function that returns how many times an item appears in database  $D$ . Then, for any two items  $o_i, o_j \in D$ :

$$o_i <_D o_j = \begin{cases} true & \text{if } s(o_i) > s(o_j) \\ true & \text{if } s(o_i) = s(o_j) \wedge o_i <_a o_j \\ false & \text{otherwise} \end{cases} \quad (1)$$

where  $<_a$  stands for alphabetic order. Equation 1 provides the definition of a *total* order operator  $<_D$  based on frequency. Based on  $<_D$ , we define the *sequence form*,  $sf$ , of a set-value.

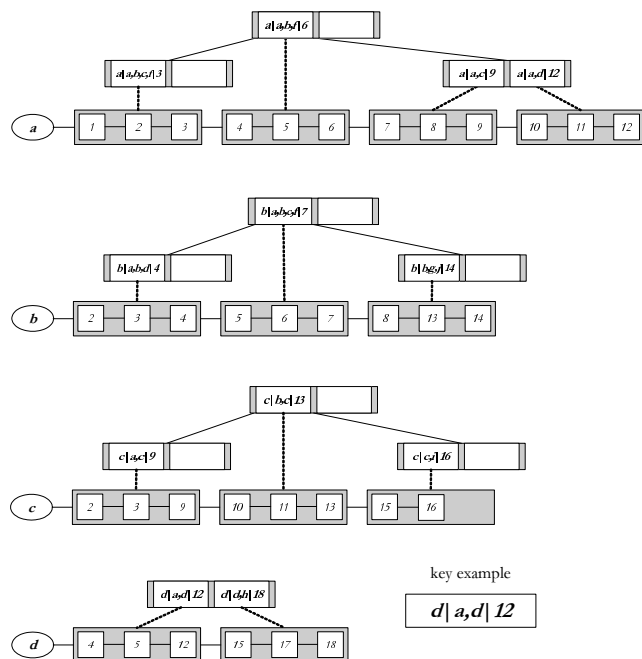


Figure 4: Partially shown OIF for data of Fig. 3.

**DEFINITION 1.** Given a set-value  $v$  from a database  $D$ , with  $n$  items we define as the sequence form of  $v$ , sequence  $sf(v) = o_1, \dots, o_n$  where  $o_i <_D o_j$  for  $i < j$ .

Consequently, the set-values are ordered *lexicographically*, after considering their  $sf$  and comparing their contents using the  $<_D$  operator. The empty set comes first in this order, followed by the set containing the smallest item in the  $<_D$  order. Following this lexicographic order, we can assign new ids to the records in  $D$  that can enhance search performance, as we discuss later. Fig. 3 shows the database of Fig. 1 after the records have been ordered and assigned a new id. This way, for two records  $t_1, t_2$ , with  $t_1.id < t_2.id$ , holds that  $sf(t_1.s) \leq sf(t_2.s)$  in the lexicographic order. Depending on the requirements of the application, we can create these ids in two ways: (a) by using intermediate arrays that associate logical ids with physical links or (b) by placing the records themselves sequentially in the hard disk following the new order; in this case we can directly treat the physical links as ids. In the latter case the ids of Fig. 3 are enough to directly access the records, in the former the ids of Fig. 3 must be “translated” to physical addresses in order for a record to be retrieved. This is often the way simple inverted files work [15].

In the sequel, for simplicity, we drop the subscript  $D$  when referring to the order between items or sets. For example,  $o_i < o_j$  implies  $o_i <_D o_j$  and  $t_i.s < t_j.s$ , implies that the sequence form of set  $t_i.s$  is lexicographically smaller than  $sf(t_j.s)$ , with respect to  $<_D$ . In addition, when we refer to a specific set-value, we list the items in it, in their  $<_D$  order. For example, when referring to set  $\{o_i, o_j\}$ , it is implied that  $o_i < o_j$ .

**Tagging for inverted lists.** Knowing that records are referenced in lexicographic order (based on  $<_D$ ) in the inverted lists can hint towards the contents of these records and whether they can contain results to a given containment query  $qs$ . Details on how containment queries are evaluated using the OIF will be provided in Section 4. To facilitate search, we consider the inverted list as a

sequence of blocks, and we employ a *tagging* mechanism that provides the lower bound for each such block. Each block is associated with a tag, which is the  $sf$  of the last record that is referenced in the block. This way, we can avoid fetching the next block from the hard disk, if we can infer that it is unnecessary. For example, consider an inverted list, which contains a block with record ids 7, 8, 9 of Fig. 3. The tag of this block is  $\{a, c\}$ , i.e., the contents of the last record (9) in the block.

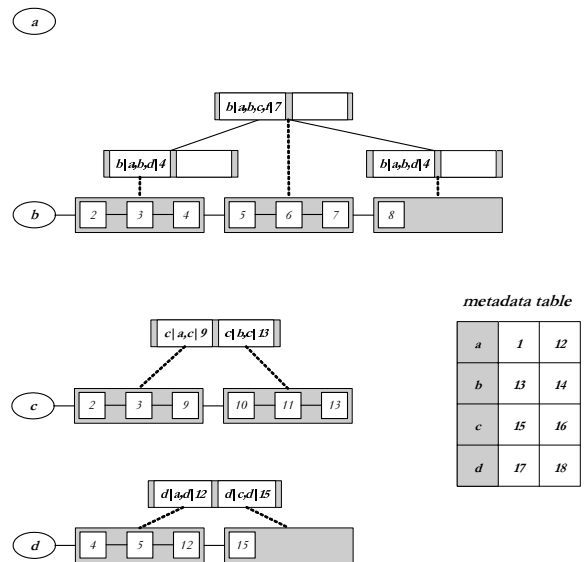
**B-tree indexing for inverted lists.** In the classic inverted file the list is simply positioned in sequential disk pages (in the ideal case). Since the tagging mechanism allows for pruning parts of the inverted list during query evaluation, the OIF provides direct access to intermediate points of the inverted list. To this end, each list is broken in blocks that are organized in a B-tree. The B-tree stores blocks by exploiting the associated tags in the key definition. Each entry in the B-tree has four parts: (a) the item that is associated with the inverted list, (b) the tag and (c) the id of the last record of the block, which form the *key* and (d) the associated block. The record-id serves two purposes: (a) it guarantees that each key will be unique and (b) we use it to speed up query evaluation (we give details in Section 4). Constructing the key in the previous way guarantees that all the blocks that belong to one list will be sequential entries in the B-tree. A part of the OIF for the database of Fig. 1 is depicted in Fig. 4. We do not place the block inside the graphical B-tree node, but instead we trace the link between the key and the block by a dotted line for reasons of readability. Moreover, we depict each inverted list indexed by a different B-tree, instead of having one single B-tree for all blocks as in the actual implementation. In the actual implementation we store all blocks in a single B-tree (since we use a single relation in the BerkeleyDB). Using the item id as a prefix to the key guarantees a unique key for each block.

Each block of the inverted list introduces only one entry to the B-tree. The size of each key depends on the average cardinality  $n$  of the set-values. Assuming each item and record-id occupies  $k$  bytes, each key takes  $(n + 2) \times k$  bytes. This size can be reduced, by (i) compressing the inverted lists and reducing the required number of blocks, and (ii) considering prefixes of the ordered set-values used as tags.

**Metadata.** An interesting consequence of assigning ids to records according to the order we introduced in Equation 1, is that the combinations of the most frequent items of each record define a contiguous region over the id space. For example, all the records whose smallest (i.e., most frequent) item is  $o$  are assigned successive ids in the id space. It is this item,  $o$ , that plays the most important role in the placement of the record in the total order of  $D$ . Based on the previous discussion, we can easily show the following theorem:

**THEOREM 1.** *For each item  $o$ , we can identify a contiguous region  $[l, u]$  in the id space which corresponds to only and all records whose smallest item is  $o$ .*

This theorem allows us to reduce the size of the inverted lists; instead of indexing all the ids of the records whose smallest item is  $o$  in the inverted list of  $o$ , we simply store the boundaries  $[l, u]$  of the region that contains them. The smallest the item  $o$  is in the total order of  $I$ , the greater the effect of keeping only the boundaries  $[l, u]$  will be; if  $o = a$  then all the records who contain  $a$  will reside in  $[1, u_a]$ , since there is no item that is smaller than  $a$ . If  $o = b$ , then in  $[l_b, u_b]$  the ids of all records that contain  $b$  and not  $a$  will be included, since it is only item  $a$  that is smaller than  $b$ . Ordering the items of  $I$  as we did in Equation 1, i.e., according to their frequency of appearance, maximizes the gains of keeping only the  $[l, u]$  boundaries instead of all the ids. We store all these



**Figure 5:** Using a metadata table can reduce the OIF of Fig. 4

regions in a *metadata* table, which we consult during runtime.

The ordering also has one more interesting consequence. If  $[l, u]$  is the contiguous region that contains records whose smallest item is  $o$ , then no record with id greater than  $u$  will contain  $o$ . If  $o$  is the smallest item of the records that appear in  $[l, u]$ , all records which appear after  $u$  will have a smallest item  $o' > o$ , else they should have been contained in  $[1, u]$ . Moreover, since the  $[l, u]$  region lies at the end of the  $[1, u]$  range,  $[l, u]$  always describes the suffix of  $o$ 's inverted list in the OIF. By bookkeeping this suffix as a range  $[l, u]$  in the metadata table, we simply cut the lists shorter. An example of a more compact version of the OIF, which uses a metadata table, for the database of Fig. 3 is depicted in Fig. 5. As it will become clear in Section 4 smaller lists lead to faster query evaluation. For instance, to answer the subset query  $\{a, b\}$  using the OIF of Fig. 5, it suffices to intersect the inverted list of the least frequent item ( $b$ ) with the metadata range of  $a$ , which is cheaper than the intersection of the two lists of the OIF depicted in Fig. 4. The gains from using the metadata are substantial; for every record we avoid creating a posting for its most frequent item. Thus in terms of postings we avoid explicitly storing  $1/\bar{l}$  of the total postings kept in a simple inverted file ( $\bar{l}$  stands for the average record length in  $D$ ).

**Compression.** The most common technique for reducing I/O accesses for the simple inverted file is compression. Several compression techniques have been proposed in literature [31, 37]. Their main idea is to code the contents of the inverted lists in some variable bit or variable byte encoding to reduce storage requirements. To further enhance the effect of the encoding, they avoid storing the actual record ids in each inverted list, but instead they store the  $d$ -gaps between them; the  $d$ -gaps are the differences between sequential ids. For example the inverted list of item  $d$  as shown is Fig. 4 is  $\{2, 5, 12, 15, 17, 18\}$ ; the  $d$ -gaps would be  $\{2, 3, 7, 3, 2, 1\}$ . The benefit from this approach is that the inverted list contains smaller values, thus the variable size encodings are more efficient. In practice, compression techniques can reduce the size of the inverted file, down to 30% of the original size, which can be even smaller than the database size [48]. These techniques are directly applicable on the OIF and they have an additional benefit due to the order we adopt in Equation 1. Instead of having in each list ids from any

part of the database, we only have ids ranging from  $[1, u]$  or  $[1, l]$  if we use the metadata table, thus their average  $d$ -gaps are smaller. In our implementation we adopt a byte-wise compression scheme [44], due to its reduced CPU cost in the decompression phase.

## 4. QUERY EVALUATION

In simple inverted files, where the ids of the records have no special meaning, the answers to an arbitrary query are usually scattered throughout the inverted lists of the involved items. The evaluation of set-containment queries over inverted files, is reduced to merge joins between the inverted lists, as discussed in Section 2. Thus, in order to retrieve the query result we usually have to scan the entire lists. There has been extensive work on list intersection algorithms, that is applicable to inverted files [5, 38, 42]. The focus in these works lies in reducing the CPU cost, since they are mostly aimed at specialized systems, which answer few types of queries and can afford to have all lists in main memory. In this section we do not try to propose novel list intersection algorithms, but rather proof-of-concept algorithms that will demonstrate how OIF can significantly reduce the I/O cost in query evaluation. Most list intersection algorithms that work for the inverted file can also exploit OIF to retrieve the lists from the disk, without significant changes. Such a scenario does not reduce the effectiveness of OIF since it still reduces the I/O by retrieving only the part of the list that is related with the query. Moreover, OIF results to smaller lists due to the use of the metadata. The basic aim of our query evaluation algorithms is to offer a fair basis of comparison between the inverted file and the OIF. The experiments of Section 5 show that even if the CPU cost of a query posed against an inverted file is 0, it would still be slower than the OIF due to its increased I/O.

The OIF reduces the I/O by having the records ordered in the inverted lists as we proposed in Section 3. The ordering allows the identification of a range of record-ids that contains the answer to each query. We call this the *Range of Interest (RoI)* of the query. The knowledge of the theoretic bounds of a query's *RoI* allows the effective utilization of the B-tree; instead of accessing the complete inverted lists, we use the tree to locate and access only the blocks that contain candidate results.

The algorithms for the evaluation of the subset, set-equality and superset queries against a database indexed by an ordered inverted file have two basic steps:

1. The identification of the *RoI*.
2. The merge-join of the inverted list regions that cover the *RoI*.

The most significant difference from the evaluation of the same queries against classic inverted files lies at the first step. Using the *RoI*, the part of the inverted lists that is examined is significantly pruned. Query evaluation also benefits from the existence of the metadata, which reduce the size of the lists and consequently the amount of data to be joined. Finally, the join exploits the direct access to different blocks provided by the B-tree. During query evaluation the candidate solutions might be limited to a region smaller than the *RoI*. Using the B-tree we can access only this region, further increasing the pruning done by the *RoI*.

The bounds of the *RoI* can be computed based only on  $qs$  and the type of the query predicate. Having identified them, we know the broadest possible region of the search space that contains the answer. Using the B-tree we can trace the sequence of blocks whose tags cover the *RoI*, without accessing the whole inverted list. The first block of this sequence is the first block in the list that has a tag greater or equal to the lower bound of the *RoI* and the tag

of the last one must be strictly greater than the greater bound of the *RoI*. For reasons of simplicity we overload the notation of *RoI* to also denote the sequence of blocks that covers the actual *RoI* in the description of the algorithms.

In the rest of this section, we present the evaluation algorithms for each query predicate and we define the *RoI* for each case. Moreover, we show that examining the *RoI* is adequate to trace the entire answer to each query. The proofs of the theorems are straightforward in all cases so we refer the interested reader to [39] for further details.

### 4.1 Subset queries

We define  $RoI_{sub}$ , i.e., the *RoI* for subset queries as follows:

**DEFINITION 2. ( $RoI_{sub}$ )** Given a subset query  $qs = \{o_{q_1}, \dots, o_{q_n}\}$ ,  $o_{q_1} < \dots < o_{q_n}$  containing items from a domain  $I = \{o_1, \dots, o_N\}$  with  $o_1 < o_2 < \dots < o_N$ , the Range of Interest  $RoI_{sub}$  is a region with the lower bound being set to  $\{o_1, o_2, \dots, o_{q_n}\}$  and the upper bound set to  $\{o_{q_1}, o_{q_2}, \dots, o_{q_n}, o_N\}$ .

**THEOREM 2.** It is sufficient to search for records within  $RoI_{sub}$  to answer a subset query.

Assume, for example, that  $I = \{a, b, \dots, j\}$  and we would like to retrieve all the records that contain  $qs = \{b, c\}$  from the relation of Fig. 1. Then,  $RoI_{sub} = [(a, b, c), (b, c, j)]$ . Any record  $t$  with  $t.s < \{a, b, c\}$  does not contain  $c$  and any record  $t'$  with  $t'.s > \{b, c, j\}$  lacks  $b$  or  $c$  or both.

The algorithm for evaluating subset queries is depicted in Algorithm 1. The evaluation starts by joining the smallest inverted lists, which belong to the greatest items (i.e., least frequent ones). This is done in order to detect possible void answers faster and to avoid having a large number of candidate solutions. At each step, the algorithm performs 2-way merge intersection join between the candidates and the current list. Each join can only reduce the number of candidates, since valid solutions need to appear in all the inverted lists. Knowing that during query evaluation we are only going to dismiss candidate solutions and not to discover any new ones allows for further pruning. We can progressively limit the range of the list that we are going to examine (initially, equal to  $RoI_{sub}$ ) considering the minimum and the maximum candidate ids. For example, if our candidates are  $\{4, 6, 9, 12\}$  then we only need to examine the part of the remaining inverted lists that contains ids in the  $[4, 12]$  range. If after the next intersection join the remaining candidates are  $\{4, 6, 9\}$  we can further limit this range to  $[4, 9]$ . The candidates are kept as in a sparse set representation in memory (i.e., as a bitset or list depending on the number of candidates). Intersections are then performed as bitwise joins or merge joins.

The direct effect of using the metadata in the evaluation of the subset queries is basically limited to the smallest (i.e., the most frequent) item (lines 11-14 of Alg. 1). For all other items, the part of the list that is described solely by the metadata is always out of the *RoI*. For example, the metadata range of item  $c$  is irrelevant to query  $qs = \{b, c\}$ , because this range contains records that have  $c$  as their smallest item (and therefore cannot contain  $b$ ). Therefore, the evaluation of a subset query  $qs = \{o_{q_1}, \dots, o_{q_n}\}$  using the metadata, follows the lines of Algorithm 1, however, the inverted list of  $o_{q_1}$  needs not be accessed; it suffices to intersect the current candidate set with the metadata range of  $o_{q_1}$ .

The worst case for the OIF is to examine the complete lists of the  $qs$  items, if the  $RoI_{sub}$  fails to prune any block. To estimate the part of each inverted list that is accessed during subset evaluation, one has to estimate the placement of the  $RoI_{sub}$  in the ordered records. The lower bound of the  $RoI_{sub}$  is always positioned

---

**Algorithm 1** Subset Query Evaluation

---

```
subset( $qs = \{o_{q_1}, \dots, o_{q_n}\}, o_{q_1} < \dots < o_{q_n}$ )
1: determine  $RoI_{sub}$ 
2: retrieve  $candidates = l_n \cap RoI_{sub}$   $\triangleright$  we insert to candidates the part of  $l_n$ 
   that falls in  $RoI_{sub}$ 
3: for all  $o_i \in (qs \setminus o_{q_n})$  do  $\triangleright$  we take items from  $qs$  in reverse order, i.e.
    $o_{q_{n-1}}, \dots, o_{q_1}$ 
4:    $range = RoI_{sub}$ 
5:   for all (blocks  $b_i$  in  $range$ ) do  $\triangleright$  we access blocks  $b_i$  from the list of  $o_i$ 
   sequentially.
6:     for all postings  $c_i$  in  $candidates$  do
7:       while posting  $p$  from  $b_i$   $p < c_i$  do
8:         get next posting  $p$  from  $b_i$ 
9:         if  $p \neq c_i$  then
10:          remove  $c_i$  from  $candidates$ 
11:     if  $o_i == o_1$  then
12:       for all remaining postings  $c_i$  in  $candidates$  do
13:         if  $c_i$  not in metadata bounds then
14:           remove  $c_i$  from  $candidates$ 
15:      $range = [lid_c, uid_c]$   $\triangleright lid_c$  is the id of the first item in  $candidates$ 
   and  $uid_c$  is the id of the last
16: return  $candidates$ 
```

---

very near to the start of the list, so the pruning depends mainly in the placement for the upper bound. For a  $qs = o_{q_1}, \dots, o_{q_n}$  this bound is  $RoI_u = o_{q_1}, \dots, o_{q_n}, o_N$ , where  $o_N$  is the last item of  $I$ . Since the order of records is lexicographical the most important term in the formula is the first. An immediate consequence of this is that the greater the least item of  $qs$  is, the worse the  $RoI_u$  will be, and thus the pruning result from the  $RoI$  will be limited. On the other hand, in a skewed distribution, an item that is big in  $I$  will be infrequent and its inverted list small, thus the subset query evaluation for a  $qs$  where all the items are big in  $I$  will be computationally cheap (if the smallest item is big in  $I$ , then all the record's items will be big in  $I$ ). In other words, the greater the inverted lists that must be accessed during query evaluation are, the greater the pruning provided by the  $RoI$ , will be.

## 4.2 Equality queries

While in the classic inverted file equality queries have similar evaluation cost to subset queries, in the case of the OIF they are significantly less expensive to compute. The range of interest  $RoI_{eq}$ , for the set equality query is a single point in the search space. We define it as follows:

**DEFINITION 3. ( $RoI_{eq}$ )** Given an equality query with a query set  $qs$ ,  $RoI_{eq}$  is a continuous region with lower and upper bound the query set  $qs$ .

Intuitively, to evaluate an equality query, we trace the blocks in each inverted list that contain the answer via the B-tree and merge-join them. The evaluation algorithm is virtually the same with the subset evaluation algorithm depicted in Algorithm 1. The basic difference is that now we use the  $RoI_{eq}$  and that we filter records according to their set-length, which is stored in the inverted lists; only records that have length equal to the query cardinality are considered in the merge join.

When the data are indexed by a classic inverted file, the worst case (which is also the most common one) for the equality queries is the same as for the subset query; the entire inverted lists have to be examined. In the average case, query processing is slightly faster than in subset queries due to the usage of the length as an additional filter. The  $RoI_{eq}$  practically defines a single block in each list, i.e.,  $|qs|$  entries in the B-tree. The only exception to this happens when there exist enough duplicates of the  $qs$  that do not fit in a single block, and take up several blocks on the index. Moreover the list of the smallest item in the query needs not be accessed at

all, since all the valid answers must lie inside the bounds traced in the metadata table for this item. As a result, the evaluation of the equality queries with OIF depends linearly on the size of the query set  $|qs|$  and only logarithmically to the size of the inverted lists and consequently to the size of  $D$ . The logarithmic dependence is due to the traversal of the B-tree, which takes place in the process of deciding the  $RoI_{eq}$  of the query. Thus the cost of evaluating an equality query is  $O(|qs| \log_b(\frac{|D|}{b_c}))$ , where  $b$  is the order of the B-tree and  $b_c$  is the number of postings that fit in a block.

## 4.3 Superset queries

Superset queries return records that include only items that belong to the query set (i.e., the record is a subset of the query set). A superset query is equivalent to  $2^{|qs|}$  equality queries. Defining the Range of Interest as  $2^{|qs|}$  distinct points is not efficient, thus we group them in larger areas, based on the first (i.e., most significant in the ordering) item of each combination. Unlike the case of the subset and equality queries, the Range of Interest for a superset query is different at each inverted list. This follows from the fact that each inverted list contributes to a partly different set of solutions (i.e., all the solutions that contain the associated item), since in superset it is not required that all the  $qs$  items are present in all lists, as in the previous queries.

**DEFINITION 4. ( $RoI_{sup}$ )** Given a query set  $qs = \{o_{q_1}, \dots, o_{q_n}\}$ , where  $o_{q_1} < \dots < o_{q_n}$  the  $RoI_{sup}$  is defined as

$$\begin{aligned} RoI_{sup-o_{q_1}} &= [(o_{q_1}), (o_{q_1}, o_{q_n})] \\ RoI_{sup-o_{q_2}} &= [(o_{q_1}, o_{q_2}), (o_{q_1}, o_{q_2}, o_{q_n})], [(o_{q_2}), (o_{q_2}, o_{q_n})] \\ &\vdots \\ RoI_{sup-o_{q_n}} &= [(o_{q_1}, \dots, o_{q_n}), (o_{q_1}, o_{q_n})], \dots, [(o_{q_n}), (o_{q_n})] \end{aligned}$$

Intuitively, in the list of the smallest item  $o_{q_1}$  of  $qs$  we identify the region of all records whose smallest item is  $o_{q_1}$ . In the list of the second smaller item of  $qs$ ,  $o_{q_2}$  we identify two regions of interest: one that contains the records where the smallest item is  $o_{q_1}$  and one with records whose smallest item is  $o_{q_2}$ . For  $o_{q_3}$ , we identify three such regions and so on. The benefit of this region definition is that the last region always falls in the range of ids stored in the metadata table and not in the inverted lists, thus it is a lot cheaper to verify if an id is included or not in it.<sup>1</sup> In Fig. 6, the  $RoI_{sup}$  for the case of  $qs = \{a, c, f\}$  is depicted. To make it more easily interpretable we represent the records with all their items (instead of their ids) and we depict all the bounds of the regions like existing records.

The algorithm for evaluating superset queries with the OIF index is depicted in Algorithm 2. The evaluation of superset queries is more expensive than the evaluation of subset and equality queries, because candidates do not get disqualified just for not appearing in one inverted list. To decide that a certain record is a valid solution, it must appear in the inverted lists of  $qs$  as many times as its length,

<sup>1</sup>A subtle problem arises from the fact that we do not trace the length of the sets in the metadata. This problem is actually limited only to records of size 1. Since the regions stored in the metadata have no overlap, it is certain that if a record contains more than 1 items, a posting containing its id and size should appear in at least one more list. If this id qualifies as a solution for the superset query, then the evaluation algorithm must have examined it and it must know its set cardinality. Finally, it is easy to solve the problem of records that contain only one item by adding one more field in the metadata table; the upper bound  $u_1$  of the region  $[l, u_1]$  which corresponds to ids of the records that contain only one item. This region will always lie in the beginning of  $[l, u]$ .

---

**Algorithm 2** Superset Query Evaluation
 

---

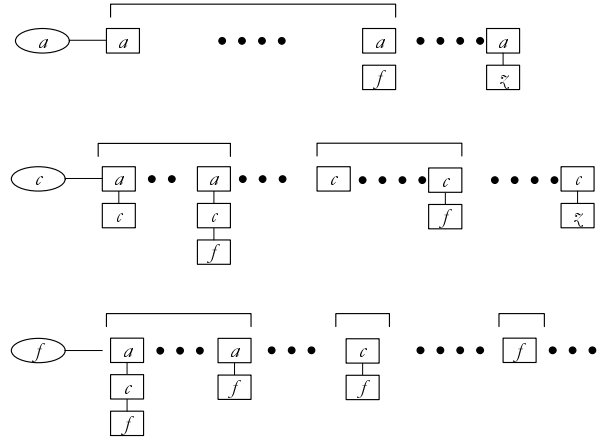
```

superset( $qs = \{o_{q_1}, \dots, o_{q_n}\}, o_{q_1} < \dots < o_{q_n}$ )
1: determine  $RoI_{sup}$   $\triangleright$  we use  $RoI_{sup-i}^j$  for the  $j$ -th  $RoI$  of item  $i$ 
2: retrieve  $candidates = l_n \cap (RoI_{sup-n}^1 \cup \dots \cup RoI_{sup-n}^n) \wedge length \leq |qs|$ 
    $\triangleright$  we retrieve the part of the list  $l_n$  of  $o_n$  that falls in  $RoI_{sup-n}$  and have
   record length less or equal to  $|qs|$ 
3:  $results =$ 
4: for all  $o_i \in (qs \setminus o_n)$  do  $\triangleright$  we take items from  $qs$  in reverse order, i.e.
    $o_{n-1}, \dots, o_{i+1}$ 
5:    $range = RoI_{sup-i}^1$ 
6:   for all (blocks  $b$  in  $range$ ) do  $\triangleright$  we access blocks  $b$  from the list of  $o_i$ 
   sequentially.
7:     for all (postings  $p$  in  $b$ ) do
8:       get next  $c$  from  $candidates$ 
9:       while ( $c < p$ ) do
10:        if ( $c.length - c.found > |qs| - i$ ) then
11:          remove  $c$  from  $candidates$ 
12:          get next  $c$  from  $candidates$ 
13:        if ( $p > c$ ) then
14:          if ( $p.length \leq |qs| - i$ ) then
15:            insert  $p$  in  $candidates$ 
16:        else
17:           $c.found++$ 
18:          if ( $c.length = c.found$ ) then
19:            remove  $c$  from  $candidates$ 
20:            insert  $c$  in  $results$ 
21:           $range = RoI_{sup-i}^x$   $\triangleright RoI_{sup-i}^x$  is the next  $RoI$  of  $i$  which is not
            covered by the previously examined block  $b$ 
22:          if ( $range = RoI_{sup-i}^n$ ) then  $\triangleright$  if it is the last  $RoI$  for  $i$ 
23:            insert all the ids that lie in  $[l, u_1]$  to  $results$ 
24:            increase the  $found$  counter for all candidates that appear in  $[u_1, u]$ 
25: return results
  
```

---

i.e., all its items must appear in  $qs$ . We can discard a candidate only if it has missed enough matches in the examined inverted lists, and safely decide that it contains additional items to those that appear in  $qs$ . To this end, for each candidate  $c$  we keep the additional information  $c.found$ , marking the number of times we encountered  $c$  in the examined inverted lists. After examining each list, we check if the total items of  $c$  that have not yet been found (i.e., the difference between the length of the record  $c.length$  and those already found,  $c.length - c.found$ ) are more than the remaining unexamined inverted lists. If this holds, then we can safely discard  $c$  as a candidate, since it contains at least one item that does not appear in  $qs$ . Unlike the case of subset and equality queries, where each successive merge-join only disqualifies candidates, here, joining the candidates with additional inverted lists can result in an increase to the candidate members. Actually, all entries that fall inside the  $RoI_{sup}$  should be inserted in the candidates, except the case where we can conclude from their length that they cannot be valid solutions. When the algorithm has completed the join of the lists, it has to examine the ids from the metadata table. Again, it increases the  $found$  counters of existing candidates that were found. No new candidates will be inserted from this region, except those having length one. Those containing multiple items should have already been inserted to candidates, since the additional items can only be greater than the one currently examined. Finally, before asking for the blocks that are contained in the next  $RoI_{sup}$  of the same inverted list, the algorithm checks if this  $RoI_{sup}$  is not already included in the previously retrieved block. Such might be a common case for small inverted lists.

The basic steps of the algorithm for evaluating superset queries are common both for classic inverted files and for ordered inverted files. Their performance is differentiated due to the ability of the OIF to limit its search to a limited part of the inverted list and its ability to exploit the metadata table. A coarse bound for the  $RoI$ 's in each inverted list is the range between  $(o_{q_1}, o_{q_i})$  and  $(o_{q_i}, o_{q_n})$ , where  $o_{q_i}$  is the item that is linked to the inverted list,  $o_{q_1}$  is the



**Figure 6:** The ranges of interest for the superset query  $\{a, c, f\}$ .

first item of the query set and  $o_n$  the last. As a general result we have two conclusions: (a) the closer the items are placed in the order of  $I$ , the more selective the  $RoI$  will be, and (b) the smaller the  $o_1$  is, the smaller the  $RoI$  will be. Moreover, due to the usage of the metadata, the inverted lists stop before the appearance of the first record whose smallest item is  $o_{q_i}$ . The remaining records are examined by using the bounds  $[u_1, u]$  for item  $o_{q_i}$  from the metadata table (see lines 23–25).

#### 4.4 Updates

A requirement for the inverted file to work efficiently is to store the inverted lists in a contiguous way on the secondary storage. This requirement leads update techniques that rely on batch, offline procedures. A popular technique for making new records instantly available is to construct a second, small, memory-resident inverted file and index them there, until the batch update takes place. The main difference between updating the OIF and the classic inverted file lies at the need to sort the data in order to provide new ids. This extra cost in the update procedure makes updating the OIF a more costly procedure than updating the classic inverted file, but still, the difference is not such that limits the applicability of OIF. In our experiments, OIF has 3-5 slower update times than IF and it behaves practically linearly to the update size as IF does. Due to space limitations we do not include the update details and experiments in the paper. They are available in the long version of the paper [40].

### 5. EXPERIMENTAL EVALUATION

We evaluated the performance of the proposed OIF index by comparing it to the state-of-the-art for containment queries, the inverted file (IF). We implemented the two indexes in C++, using Berkeley DB as our storage engine. Berkeley DB supports relations that have two fields: key and data. There is no type restriction for any of the fields and they can be any binary object. In our implementations each block is stored at the data field of the relation. In the implementation of the OIF, we split the inverted lists into blocks, which are stored as independent entries in the relation, with a B+–tree primary organization. Each block is associated with a key that is formed by combining the item that is associated with the list and the content of the last record (i.e., the tag), together with its id. Each inverted list is populated by postings which are comprised by the id and the length of the records. The ids are represented as series of  $d$ -gaps compressed by a  $v$ -byte compression. The same

compression is used for the lengths of the records.

For the IF, we use the most efficient implementation scheme reported [29]: each tuple has as key value an item  $o$  from  $I$  and as data value the whole inverted list that is associated with  $o$ . The relation is indexed by a hash over the key values. The postings are compressed exactly as in the case of the OIF. Note that Berkeley DB always retrieves the whole tuple, i.e. there is no way to retrieve a part of the inverted list.

**Data.** We evaluated the OIF using two real datasets from UCI KDD repository [21]. The first, denoted as *msweb*, is a one-week log tracing the virtual areas that users visited in the web portal *www.microsoft.com*. There are 32K records and the vocabulary of the dataset contains 294 distinct items (areas). The distribution of the items in the records is skewed and the average size of the record is 3. To be able to draw informative conclusions on a large database, we replicated the dataset 10 times. This replication is meaningful, since it simply simulates a 10-week log from the web portal. The second dataset, denoted *msnbc* is again a log of users behavior at another web portal, *msnbc.com*, containing 990K records. The vocabulary here is very limited, comprising only 17 distinct items and unlike the previous one, the distribution of the items is relatively uniform. The average cardinality of a set-value is 5.7.

To assess the performance impact of several statistical properties, we used synthetic data containing set-values with length varying from 2 to 20. We considered datasets of 1M, 5M, 10M and 50M set-values containing items from vocabularies of sizes 500, 2K and 8K. The frequency of items in the set-values is a moderately skewed Zipfian distribution of order 0.8. Unless explicitly stated we use as default parameters a domain of size 2K and 10M records with a distribution of order 0.8.

**Queries.** As in other approaches [20], we evaluated our proposal using queries that always have an answer, considering them more informative than those that do not. We created such queries by using existing set-values, selected uniformly from all  $D$ . The selectivities of the subset queries are less than 3%, with the less selective being those with  $|qs| = 2$ . The most common case for larger  $|qs|$  and for equality queries is that there are less than 5 answers. On the other hand the selectivity of the superset queries can surpass 3% for large  $|qs|$  on the real data. To provide representative results we created 10 queries of each size and type.

**Performance evaluation.** In our experiments, we primarily evaluate the I/O cost. For this reason, we set up the database cache to the minimum (32K) and we circumvent the operating system cache. This leaves only the effect of the hard disk cache, which is limited. We minimize the effects of caching to observe more accurately how the index would scale for larger datasets, when given limited cache size. We would like to stress that the important factor is the percentage of available memory to the underlying database size: in realistic situations where the DBMS will have to simultaneously support multiple queries, the memory assigned per query is bounded. Therefore, our approach is intentionally tailored and tested to sustain bounded -in fact, small- memory budgets. We trace the actual disk page accesses, reported as cache misses by the database. Berkeley DB does not report separately sequential and random disk page accesses. The query evaluation algorithms need a few random disk page accesses to trace the beginning of the list (or of the *RoI* in the case of the OIF) in the disk, and then they retrieve sequential disk pages from the inverted list. The random disk page accesses when using the OIF are more frequent than in the case of the IF, due to the B-tree indexing and the large number of keys. Still, our experiments show that this overhead is proportional to the query size and not to the database or the domain size and its effect is quite limited. To better understand how sequen-

tial and random accesses affect the IF and the OIF we present the query evaluation time and we distinguish it in CPU and I/O time by repeatedly counting clock ticks and total time in a system where no other operation runs. We present runtimes only for the synthetic datasets which are large enough not to be significantly distorted by caching and prefetching operations by the hard disk.

**Subset.** The OIF outperforms the IF both for real and for synthetic data. Moreover, it exhibits two very good properties (see Fig. 7 and 8). As the length of the query set grows and thus, queries have fewer answers, it manages to use the B-tree efficiently and detect fast the areas of interest in each list. This way, its cost drops, unlike the case of the IF, which suffers when it has to examine many inverted lists and cannot benefit from the small selectivity. Another good property of the OIF is that it scales well as the database  $D$  grows. This is again attributed to the B-tree and the limited *RoI*. When the size of the database and consequently the size of the lists is small, the random access I/O nullifies the advantages of the OIF and the I/O cost is similar to that of the IF for the smallest dataset of 1M records. As the size of the database grows, the gains of avoiding large amounts of sequential disc accesses grow evident. As we can see the I/O time grows as the query size grows, whereas the disk page accesses remain fairly stable. This reflects the fact that the OIF needs more random accesses for detecting the *RoI* in a list, than the IF needs for detecting a list. Thus, when the number of lists increases the I/O time increases too due to the random accesses needed to find the *RoI* inside each list.

**Equality.** As expected from the complexity analysis, the cost of the OIF is practically constant (see Fig. 7 and 9), since it can access directly the small set of disk pages where the possible answer lies. In contrast, the IF does not have the opportunity to prune ids using *RoI* and, as experiments on both real and synthetic data confirm, it has significantly higher cost. Finally, the ability of the OIF to prune the candidates very effectively, results in unnoticeable CPU cost.

**Superset.** Superset allows less pruning of the lists compared to the other queries, but still the OIF systematically outperforms the IF in both real (Fig. 7) and synthetic data (Fig. 10) for all domain, database, and query-set sizes. In the real data sets, it is clear that the benefits from the OIF are not as drastic as in the two other cases; this is due to the fact that the databases and the vocabularies are rather small, so the the query-set size (and thus, the number of examined lists) is significant compared to the vocabulary. The percentage of pages examined by the OIF is still substantially lower than in the case of the IF, but the OIF is forced to do more random I/O. This is reflected on the I/O times. The random I/O accesses are again proportional to the query size, and not to the domain or the database size. The pruning power of the OIF is reflected in the smaller CPU cost, which is a result of producing less intermediate results and of the exploitation of the metadata table. The benefits are more clear in Fig. 10 if one looks at the way the IF and the OIF scale with respect to the database size. Similar observations can be made as  $qs$  increases.

For all query types, it is noteworthy that the OIF is more robust to the *skewness* of the data compared to the IF. While in uniform distributions (zipfian order = 0) the two structures perform almost equally well (with the IF having a slight advantage in the superset queries), as the skew increases, the performance of the IF quickly drops by an order of magnitude for subset and equality queries and by 25-30% for superset queries.

**Space overhead.** As explained in Section 3, the inverted lists of the OIF can be compressed as the lists of the IF, and the metadata table can be used to further reduce space requirements. In contrast, since each original list breaks to smaller ones, we need to keep the first record id of each sub-list explicitly and not as a  $d$ -gap from a



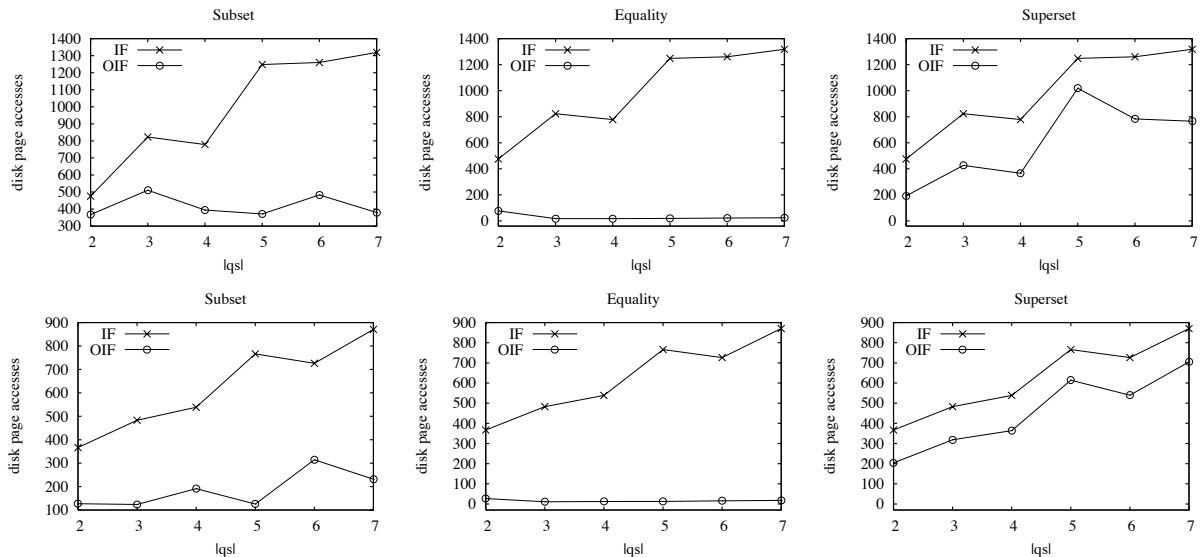


Figure 7: Average performance of queries on real datasets - First row *msweb* data and second row *msnbc* data

previous one. As a result, in our implementation, the size the inverted lists in the OIF are only marginally (5%) smaller than the IF lists. Still, the size of the Berkeley DB table for the OIF is significantly larger; the OIF occupies 35% of the space of the original data, whereas the IF occupies just 22% of the that space. The overhead of the OIF is due to several reasons: the large size of the keys (we did not use prefixes or other compression on them); the fact that we chose to have one B-tree instead of many smaller ones, one for each inverted list; and due to the B-tree fill factor. If a reassignment map is required (i.e., the record ids in the OIF are not the original ids that are used in the relation that stores the data) we would need an extra table taking 8% of the original data, raising the OIF space requirements to almost double than those of the IF (43% vs 22%). Nevertheless, as our evaluation shows, the space overhead of the OIF over the IF does negate its performance benefits.

**Impact of the OIF ordering.** An interesting question about the OIF is whether its performance is attributed to the special ordering and the metadata or to the indexing of the inverted lists. To investigate this issue we performed the following experiment. We created a B-tree for the inverted lists exactly in the same way we created the OIF (same block size) but without any ordering for the records. Moreover, we used only the record id as a key for the B-tree instead of the whole records, thus we ended up with a more compact structure compared to the OIF. The resulting unordered B-tree does not have any advantage over the OIF or the IF for superset queries, since the scanning of the whole lists cannot be avoided at each iteration of Algorithm 2. For equality queries (with small selectivities) both the OIF and the unordered B-tree have a similar performance since the candidate solutions are usually very limited and can be directly accessed using the B-tree. The most interesting case is that of the subset queries. We performed an experiment on our default synthetic dataset varying the query selectivity from  $10^{-7}$  (only 1 answer) to  $10^{-2}$ . The results showed that the OIF outperforms the unordered B-tree on the inverted lists in all cases. Due to space limitations we do not detail the experiments here but we refer the interested reader to the long version of the paper [40]. This experiment throws also light to the relation between the OIF and the other structures that offer access to intermediate points in the

verted lists, e.g., skip lists. The ordering and the metadata of the OIF provide a benefit that is orthogonal to the indexing of the lists and other indexing schemes for the lists can benefit for them.

**Performance summary.** With faster query evaluation and slower update times (see [40] for the updates' performance), OIF offers a different tradeoff between performance and maintenance compared to the IF. In the example of the dataset with 1M records from a domain of 2000 items, the average query evaluation time (for all three predicates together) took 133 msec for the IF and 25 msec for the OIF. On the other hand inserting 200K records in the same dataset took 12 sec for the IF and 27 sec for the OIF, which results to an average of 0.06 msec per record for the IF and 0.135 msec per record for the OIF. This implies that a workload with a ratio of updates to queries smaller than 766:1, would be handled faster by the OIF. Common applications that use inverted files are not update-intensive, i.e., queries are more frequent than updates, therefore the increased update cost of the OIF, compared to the IF is gracefully compensated by the great gains in query performance.

In summary, the OIF significantly outperforms the IF in all query cases. The benefits systematically become more clear as the fraction of the database over the domain grows (and the lists of the IF become longer, while the OIF is constrained to few pages due to the appropriate *RoI*). This is evident both when the database size increases and when the domain is quite small. As a tradeoff to this the OIF is slower than the IF in updates and has increased space overhead, but this disadvantage is leveraged by the fact that in both cases the updates have to be done in a batch manner and also by the small amortized cost of the updates compared to query evaluation.

## 6. RELATED WORK

**Set-containment queries.** Research on set containment queries in a database context has been limited [17, 20]. Recently, there has been work on error-tolerant set-containment queries [1], which lie closer to similarity queries. Moreover, the authors of [1], differently from our context, focus mostly on main-memory evaluation and not on disk resident indices. The most basic results for containment queries stem from the Information Retrieval (IR) and text databases areas. In these areas, containment is considered in the

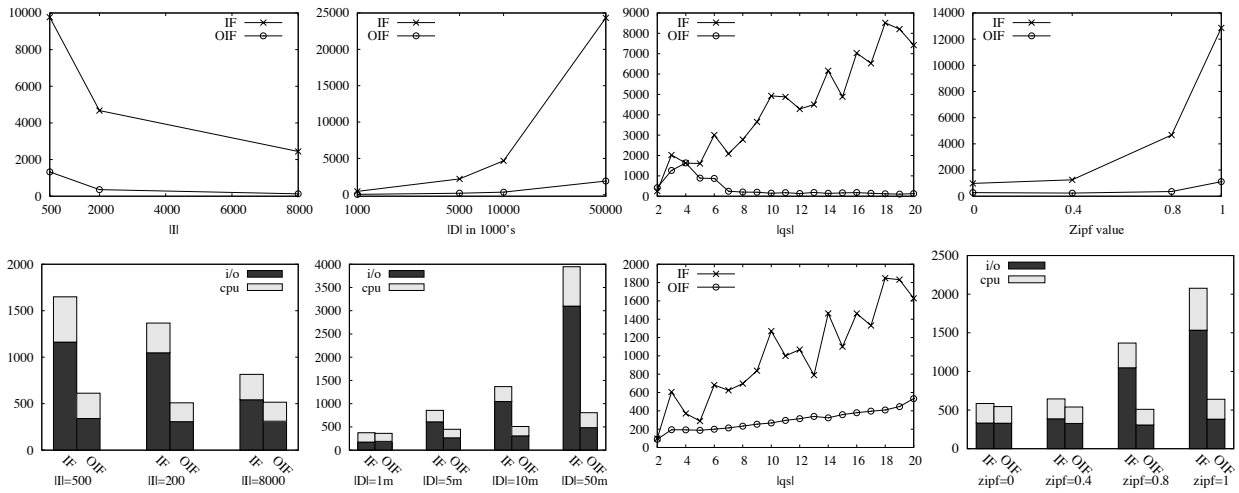


Figure 8: Average performance of subset queries on synthetic datasets - First row shows disk page accesses and second row time in msec

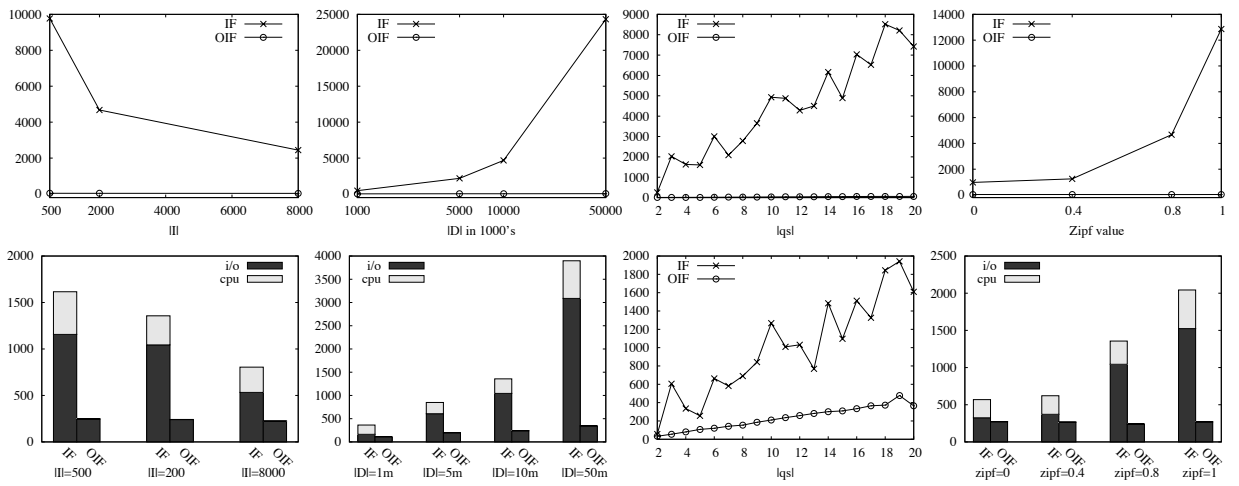


Figure 9: Average performance of equality queries on synthetic datasets - First row shows disk page accesses and second row time in msec

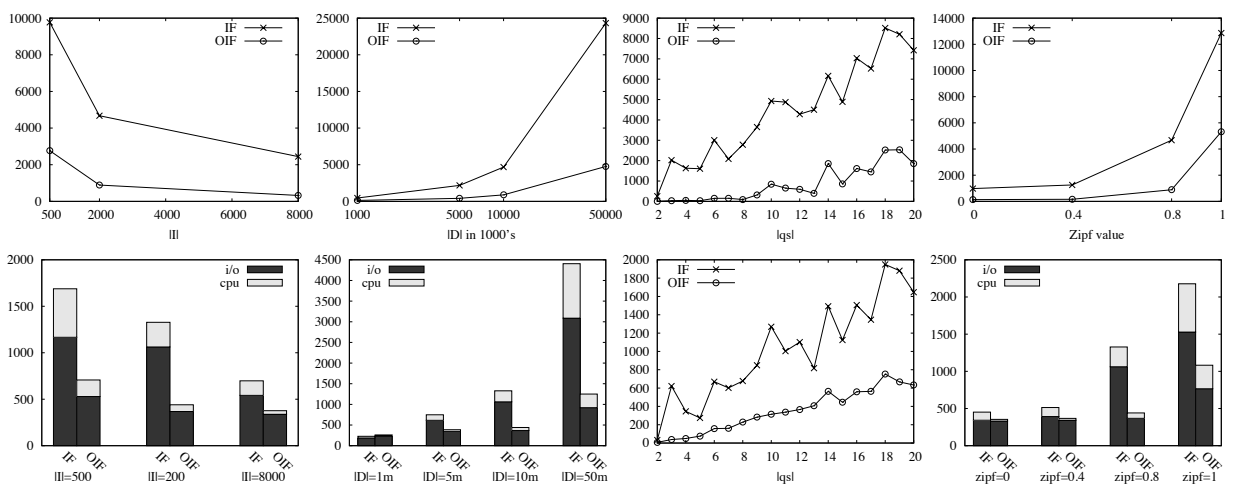


Figure 10: Average performance of superset queries on synthetic datasets - First row shows disk page accesses and second row time in msec

context of text documents in natural language. The most profound example is the case of WWW search engines, where web documents that contain<sup>2</sup> the query terms that have been provided by the user, are retrieved from a collection of millions of web pages. Research in the database field has given more focus on set-containment joins [6, 27, 30, 35, 36, 43] and similarity queries [16, 28] and less on simple containment evaluation as we do in this paper.

**Inverted files.** Inverted files [24, 49] are the indexing solution employed by all WWW search engines and the most efficient index structure for text query evaluation in research literature. In terms of *storage allocation*, the most effective physical storage allocation scheme for inverted lists is to store them contiguously in the disk [47]. Alternatives in the research literature and in practice are motivated by the difficulty to support contiguous storage in the case of updates. To deal with *maintenance operations* efficiently, alternative approaches either overallocate space for future updates or split the long lists of the inverted file in smaller chunks of disk pages, stored contiguously in the disk. All strategies that require that the inverted lists are stored contiguously, store the updates initially in a main memory inverted file. When the available memory gets full, it is necessary to move all the postings from the main memory to disk. This way we only do batch updates in a frequency depending on the rate of updates and the available memory buffer [47]. Several enhancements of the inverted files rely on treating long and short inverted lists differently. Having lists that vary substantially in size, is a result of skewed item distributions in the database, which is a common real world case. The Hybrid Trie Inverted file (HTI) [41], breaks up the larger inverted lists to smaller sublists that contain known combinations of items. This approach provides superior performance over the inverted file for skewed distributions (a comparison with OIF appears in [39]). In [25], König et. al. propose a index structure that similarly to HTI creates inverted lists for combinations of items. It balances the number of indexed item-combinations with the length of the lists, using a cost-model for main-memory access to trade off between these two factors. It is not directly comparable to OIF since it is memory resident and focus only on a specific query (i.e., superset). Finally, in [7] the authors propose an indexing scheme for containment queries that also relies on keeping inverted lists for frequent term combinations, but it is focuses on indexing natural language text documents. Through the suitable choice of term combinations the authors manage to keep the size of the resulting index comparable to the size of a simple inverted index.

**Signatures.** Signature files [13, 14] are the basic alternative method to the inverted file and traditional RDBMS methods for containment queries. The main idea behind signatures is to hash each item of  $I$  to a fixed size word and then to *superimpose* the codes of all the items of a record, to create the records' *signature*. Superimposing relies usually to the usage of some binary operation (*AND*, *OR*, *XOR* etc) between two signatures. Apart from the traditional signature approaches, the indexing of signatures has also been explored in the literature, with the most prominent idea being the signature trees [12, 28, 8, 32]. Signatures trees organize the records' signatures following the same lines as  $R$ -trees and  $B$ -trees. Each node has a signature, which is the result of superimposing the signatures of its immediate descendants.

**XML search.** Inverted files have also been employed for searching semi-structured data. XML documents are as trees and their elements and values are encoded as intervals that capture the ancestor/descendant relationships in the tree hierarchy. Inverted files have been used to index the encodings of XML structural elements

in order to efficiently answer XML path and twig queries, which can be modeled as containment joins between the intervals [2, 46]. Follow-up research [23] has shown that indexing the inverted lists can further improve performance. The XML indexing problem for path query evaluation is essentially different to the classic set containment search problems we study in this paper and OIF is not comparable to XML indexes, structurally or operationally.

**Alternative organizations for inverted lists.** Special orderings for the postings in inverted lists have been studied in several contexts. In [33] the postings are sorted according to the in-document frequency of each term and in [3, 4, 19] the sorting criterion is the normalized in-document frequency. These approaches focus on the evaluation of IR queries, which require ranking of the results. Ranking queries benefit from these orderings, since most IR similarity measures are directly affected by the in-document frequency of each term. During the evaluation, the algorithm exploits the ordering of the lists to retrieve the results in the desired sort order or to decide on similarity bounds which are used as thresholds for terminating the query evaluation. For similar purposes, inverted lists are sorted according to the record length in [18]. In this case, the record length is used to provide bounds for the similarity between different records. Knowing the bounds allows to limit the search in only a part of the inverted lists. The aforementioned architectures are reminiscent to the OIF, however, their organizations are not suitable for the boolean containment queries studied here [47]. A significant difference also lies in the fact that in these approaches the records are sorted locally in each inverted list, and not globally as in the case of OIF. Finally, in [9], postings are ordered by taking into account spatial information. The main objective is to support combined geographic and keyword search to web documents. Each document can be associated to one or more geographical regions on a map, based on the location of its hosting site, or location information in its content. By encoding these spatial areas in the document ids, querying for documents based on both their textual content and spatial proximity to a location of interest is possible (e.g. find all documents about "yoga" which are associated to locations near Brooklyn). The inverted lists corresponding to the textual query terms are intersected, but regions in these lists that contain document ids not related to the spatial query component are not accessed. A problem of the previous approaches is that they reduce the effectiveness of compression techniques, since they lead on larger average  $d$ -gaps [47].

**List Intersection.** Although in this work we focus on the index structure, relevant work to the query evaluation part appears in the literature concerned with list intersection algorithms. In [10, 11] an adaptive algorithm for computing set intersections, unions and differences is described. The first algorithm of [11] polls each list in a round robin fashion, and it is ameliorated in [10]. In [42], the authors propose a main memory list intersection algorithm for sorted and unsorted lists. The algorithm exploits the characteristics of modern hardware and focuses on balancing the load between multiple cores. Moreover it probes the lists in order to gather statistics that would allow efficient exploding of the multi-level cache hierarchy. Unlike our approach it does not deal primarily with the disk I/O. Efficient exploitation of multiple core CPU is also in the focus of [38], which proposes inter-query parallelism and intra-query parallelism. The former exploits parallelism between different queries, while the latter parallelizes the processing within a single query. Finally, [5] offers an experimental comparison of several popular methods of list intersection with respect to their CPU cost.

## 7. CONCLUSIONS

In this paper we proposed a novel indexing scheme, the ordered

<sup>2</sup>The matching criteria are more complex; still containment is a vital part of the retrieval process.

inverted file (OIF). The key idea of the index is to order the data suitably to allow early pruning in query evaluation time. We have described query evaluation algorithms that take advantage of the OIF and theoretically showed that the OIF manages fewer disk page accesses and faster evaluation times than the simple inverted file. This claim has also been supported by extensive experiments on both real and synthetic data. The results show that the performance of the OIF is often orders of magnitude superior to that of the inverted file and that it exhibits good scaling properties.

We do not propose the OIF as a total replacement for the inverted file, since in a variety of applications, especially in the IR context, the individual inverted lists are not that big, and the nature of the queries does not permit skipping a significant part of the involved lists. Still, our contribution serves the purpose of answering containment queries with exact semantics, under limited memory budgets. OIF is especially efficient for large collections of records from a limited item domain, or from domains where the item's distribution is skewed. We consider the above assumptions realistic and the OIF to be a practical and superior solution, since it outperforms inverted files for all kinds of containment queries.

Future work can be directed towards the efficient evaluation of composite predicates and other type of predicates (e.g., similarity).

## 8. REFERENCES

- [1] P. Agrawal, A. Arasu, and R. Kaushik. On indexing error-tolerant set containment. In *SIGMOD*, 2010.
- [2] S. Al-Khalifa, H. V. Jagadish, J. M. Patel, Y. Wu, N. Koudas, and D. Srivastava. Structural joins: A primitive for efficient xml query pattern matching. In *ICDE*, 2002.
- [3] V. N. Anh, O. de Kretser, and A. Moffat. Vector-space ranking with effective early termination. In *SIGIR*, 2001.
- [4] V. N. Anh and A. Moffat. Impact transformation: effective and efficient web retrieval. In *SIGIR*, 2002.
- [5] J. Barbay, A. López-Ortiz, T. Lu, and A. Salinger. An experimental investigation of set intersection algorithms for text searching. *J. Exp. Algorithmics*, 14:3:7–3:24, 2009.
- [6] J.-Y. Cai, V. T. Chakaravarthy, R. Kaushik, and J. F. Naughton. On the complexity of join predicates. In *PODS*, 2001.
- [7] S. Chaudhuri, K. W. Church, A. C. König, and L. Sui. Heavy-tailed distributions and multi-keyword queries. In *SIGIR*, 2007.
- [8] Y. Chen. On the signature trees and balanced signature trees. In *ICDE*, pages 742–753, 2005.
- [9] Y.-Y. Chen, T. Suel, and A. Markowetz. Efficient query processing in geographic web search engines. In *SIGMOD*, 2006.
- [10] E. D. Demaine, L.-O. Alejandro, and J. I. Munro. Experiments on adaptive set intersections for text retrieval systems. In *ALENEX*, 2001.
- [11] E. D. Demaine, A. López-Ortiz, and J. I. Munro. Adaptive set intersections, unions, and differences. In *SODA*, 2000.
- [12] U. Deppisch. S-tree: A dynamic balanced signature index for office retrieval. In *SIGIR*, 1986.
- [13] C. Faloutsos. Signature files. In *Information Retrieval: Data Structures & Algorithms*, pages 44–65. 1992.
- [14] C. Faloutsos and S. Christodoulakis. Signature files: an access method for documents and its analytical performance evaluation. *ACM Trans. Inf. Syst.*, 2(4):267–288, 1984.
- [15] W. B. Frakes and R. A. Baeza-Yates, editors. *Information Retrieval: Data Structures & Algorithms*. Prentice-Hall, 1992.
- [16] A. Gionis, D. Gunopulos, and N. Koudas. Efficient and tunable similar set retrieval. In *SIGMOD*, 2001.
- [17] R. Goldman and J. Widom. Wsq/dsq: A practical approach for combined querying of databases and the web. In *SIGMOD*, 2000.
- [18] M. Hadjieleftheriou, A. Chandel, N. Koudas, and D. Srivastava. Fast indexes and algorithms for set similarity selection queries. In *ICDE*, 2008.
- [19] D. Hawking. Efficiency/effectiveness trade-offs in query processing. *SIGIR Forum*, 32(2):16–22, 1998.
- [20] S. Helmer and G. Moerkotte. A performance study of four index structures for set-valued attributes of low cardinality. *VLDBJ*, 12(3):244 – 261, 2003.
- [21] S. Hettich and S. D. Bay. The UCI KDD Archive. Univ. of California, Dept. Information and Comp. Science, <http://kdd.ics.uci.edu>. 1999.
- [22] F. M. Institute. Supermarket facts & figures. [http://www.fmi.org/facts\\_figs/superfact.htm](http://www.fmi.org/facts_figs/superfact.htm), 2006.
- [23] H. Jiang, H. Lu, W. Wang, and B. C. Ooi. Xr-tree: Indexing xml data for efficient structural joins. In *ICDE*, 2003.
- [24] D. E. Knuth. *The Art of Computer Programming, Volume III: Sorting and Searching*. Addison-Wesley, 1973.
- [25] A. C. König, K. Church, and M. Markov. A data structure for sponsored search. In *ICDE*, 2009.
- [26] N. Lester, J. Zobel, and H. E. Williams. Efficient online index maintenance for contiguous inverted lists. *Inf. Process. Manage.*, 42(4):916–933, 2006.
- [27] N. Mamoulis. Efficient processing of joins on set-valued attributes. In *SIGMOD*, 2003.
- [28] N. Mamoulis, D. W. Cheung, and W. Lian. Similarity search in sets and categorical data using the signature tree. In *ICDE*, 2003.
- [29] S. Melink, S. Raghavan, B. Yang, and H. Garcia-Molina. Building a distributed full-text index for the web. *ACM Trans. Inf. Syst.*, 19(3):217–241, 2001.
- [30] S. Melnik and H. Garcia-Molina. Adaptive algorithms for set containment joins. *ACM Trans. Database Syst.*, 28(1):56–99, 2003.
- [31] A. Moffat and J. Zobel. Self-indexing inverted files for fast text retrieval. *ACM Transactions on Information Systems*, 14(4), 1996.
- [32] A. Nanopoulos and Y. Manolopoulos. Efficient similarity search for market basket data. *The VLDB Journal*, 11(2):138–152, 2002.
- [33] M. Persin, J. Zobel, and R. Sacks-Davis. Filtered document retrieval with frequency-sorted indexes. *J. Am. Soc. Inf. Sci.*, 47(10), 1996.
- [34] W. Pugh. Skip lists: a probabilistic alternative to balanced trees. *Commun. ACM*, 33(6):668–676, 1990.
- [35] K. Ramasamy, J. M. Patel, J. F. Naughton, and R. Kaushik. Set containment joins: The good, the bad and the ugly. In *VLDB*, 2000.
- [36] S. Sarawagi and A. Kirpal. Efficient set joins on similarity predicates. In *SIGMOD*, 2004.
- [37] F. Scholer, H. E. Williams, J. Yiannis, and J. Zobel. Compression of inverted indexes for fast query evaluation. In *SIGIR*, Aug. 2002.
- [38] S. Tatikonda, F. Junqueira, B. B. Cambazoglu, and V. Plachouras. On efficient posting list intersection with multicore processors. In *SIGIR*, pages 738–739, 2009.
- [39] M. Terrovitis. *Modelling and operational issues in pattern base management systems*. PhD thesis, El. and Comp. Eng., NTUA, available at <http://www.dblab.ece.ntua.gr>, 2007.
- [40] M. Terrovitis, P. Bouros, P. Vassiliadis, T. Sellis, and N. Mamoulis. Efficient answering of set containment queries for skewed item distributions. Technical Report TR-IMIS-2010-1, IMIS, 2010.
- [41] M. Terrovitis, S. Passas, P. Vassiliadis, and T. Sellis. A combination of trie-trees and inverted files for the indexing of set-valued attributes. In *CIKM*, 2006.
- [42] D. Tsirogiannis, S. Guha, and N. Koudas. Improving the performance of list intersection. *PVLDB*, 2(1):838–849, 2009.
- [43] R. Vernica, M. J. Carey, and C. Li. Efficient parallel set-similarity joins using mapreduce. In *SIGMOD*, 2010.
- [44] H. E. Williams and J. Zobel. Compressing Integers for Fast File Access. *The Computer Journal*, 42(3):193–201, 1999.
- [45] I. H. Witten, A. Moffat, and T. C. Bell. *Managing Gigabytes: Compressing and Indexing Documents and Images*. Morgan Kaufmann, 2nd edition, 1999.
- [46] C. Zhang, J. F. Naughton, D. J. DeWitt, Q. Luo, and G. M. Lohman. On supporting containment queries in relational database management systems. In *SIGMOD*, 2001.
- [47] J. Zobel and A. Moffat. Inverted files for text search engines. *ACM Comput. Surv.*, 38(2):6, 2006.
- [48] J. Zobel, A. Moffat, and K. Ramamohanarao. Inverted files versus signature files for text indexing. *ACM Transactions on Database Systems*, 23(4):453–490, 1998.
- [49] J. Zobel, A. Moffat, and R. Sacks-Davis. An efficient indexing technique for full text databases. In *VLDB*, 1992.